Differential Item Functioning Effect Size From the Multigroup Confirmatory Factor Analysis for a Meta-Analysis: A Simulation Study

Sung Eun Park, Soyeon Ahn and Cengiz Zopluoglu

Abstract
This study presents a new approach to synthesizing differential item functioning (DIF) effect size: First, using correlation matrices from each study, we perform a multigroup confirmatory factor analysis (MGCFA) that examines measurement invariance of a test item between two subgroups (i.e., focal and reference groups). Then we synthesize, across the studies, the differences in the estimated factor loadings between the two subgroups, resulting in a meta-analytic summary of the MGCFA effect sizes (MGCFA-ES). The performance of this new approach was examined using a Monte Carlo simulation, where we created 108 conditions by four factors: (1) three levels of item difficulty, (2) four magnitudes of DIF, (3) three levels of sample size, and (4) three types of correlation matrix (tetrachoric, adjusted Pearson, and Pearson). Results indicate that when MGCFA is fitted to tetrachoric correlation matrices, the meta-analytic summary of the MGCFA-ES performed best in terms of bias and mean square error values, 95% confidence interval coverages, empirical standard errors, Type I error rates, and statistical power; and reasonably well with adjusted Pearson correlation matrices. In addition, when tetrachoric correlation matrices are used, a meta-analytic summary of the MGCFA-ES performed well, particularly, under the condition that a high difficulty item with a large DIF was administered to a large sample size. Our result offers an option for synthesizing the magnitude of DIF on a flagged item across studies in practice.

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Fairness is a critical component of high-stakes testing from both ethical and legal standpoints. The Educational Testing Service (2014) considers a test to be “fair if any group differences in performance are derived from construct-relevant sources of variance. The existence of group differences in performance does not necessarily make a test unfair, because the groups may differ on the construct being measured” (p. 57). However, if an examinee’s performance on any test item is affected by construct-irrelevant characteristics (e.g., male vs. female, students with disability vs. those without disability), a test or an item is said to be biased, providing an unfair advantage for one group over others.

Differential item functioning (DIF) is a statistical character of an item that can help detect whether a test contains a systematic bias based on construct-irrelevant characteristics. DIF displays the extent to which the performance on an item systematically differs by subgroups (Osterlind & Everson, 2009). The DIF is said to be present when examinees in subgroups (e.g., race/ethnicity, gender, socioeconomic status) with the same level of latent traits have different probabilities of correctly responding to a given item. Although two types of DIF can be identified in practice—uniform DIF (constant across ability levels) and nonuniform DIF (varying across ability level), the current study particularly focuses on a uniform DIF for a dichotomous item.

In the literature, various parametric and nonparametric statistical techniques and the associated effect-size measures detecting uniform DIF have been well documented. These are the Mantel–Haenszel (MH) procedure (Camilli & Shepard, 1994; Hidalgo et al., 2014; Holland & Thayer, 1988; Zwick et al., 2012), logistic regression (LR) modeling (Gómez-Benito et al., 2009; Hidalgo et al., 2014), item response theory (IRT)–based method (Oshima et al., 2015; Raju, 1988; Steinberg & Thissen, 2006), structural equation modeling (SEM; Bauer, 2017; Steinmetz et al., 2009; Woods & Grimm, 2011), and variations of the aforementioned techniques (Chang et al., 1995; Penfield, 2007; Walker, 2011).

While research on DIF detection procedures and the associated effect-size measures has been proliferating in the field, literature regarding the synthesis of DIF indicators is limited. To our knowledge, of the many DIF indices discussed above, only the MH and the LR models have been examined as an effect size indicator for the meta-analyses of DIF detection on an item (i.e., Koo, 2012; Koo et al., 2014; Van de Water, 2014). Koo (2012) suggested using the MH DIF index in meta-analyses, and conducted a simulation study that examined its performance. In 2014, Van de Water conducted a simulation study that compared the Type I error rates and statistical power of using the LR and the MH DIF indices in meta-analyses. He further examined the differential effects of other study characteristics, such as sample size, test
length, and magnitude of DIF, on Type I error rates and statistical power between LR and MH in meta-analyses.

Researchers have increasingly used SEM approaches in detecting an item or a test displaying DIF among subgroups. The two most commonly used SEM approaches are the multiple indicator and multiple cause (MIMIC) and the multigroup confirmatory factor analysis (MGCFA) models. Based on the well-known parametric equivalence between the MIMIC and the IRT models (Muthén et al., 1991), Jin et al. (2012) have proposed the effect size measure for MIMIC (MIMIC-ES) as given by

\[
\text{MIMIC-ES} = \frac{\tau_i - \beta_i}{\lambda_i} = -\frac{\beta_i}{\lambda_i},
\]

where \(\tau_i\) is the threshold, \(\beta_i\) is direct effect of the grouping as a dummy variable on the latent factor, and \(\lambda_i\) is the factor loading for \(i\)th item.

Similarly, given that the parameters estimated by the MGCFA model are equivalent to item parameters estimated by the IRT model (Stark et al., 2006), the \(b\)-parameter on the \(i\)th item can be written as

\[
b_i = \frac{\tau_i}{\lambda_i},
\]

where \(\tau_i\) is the threshold for the \(i\)th item.

With the parametric equivalence of difficulty parameters between the MGCFA and IRT models, the following effect size (MGCFA-ES) can be used as an indicator that quantifies the magnitude and direction of a uniform DIF on an item between subgroups for the MGCFA model as given by

\[
\text{MGCFA-ES} = b_i^F - b_i^R = \frac{\tau_i^F}{\lambda_i^F} - \frac{\tau_i^R}{\lambda_i^R},
\]

where \(F\) and \(R\) are the focal and reference groups, respectively.

The Current Study

Given that the SEM approaches (either MIMIC or MGCFA) have been increasingly utilized, it is practically important to evaluate whether an effect size estimator derived from the SEM approaches can be used in meta-analyses. We found that studies do not always provide sample responses for each item, as would be required in a MIMIC approach. More often, studies provide correlation matrices among sample responses on items, making MGCFA-ES a more suitable and practical approach for meta-analyses. In particular, the current study assumes that two separate correlation matrices for focal and reference groups were reported in each study. From these correlation matrices, MGCFA-ES and its associated standard error can be estimated and then synthesized across studies to estimate the DIF on an item.
Specifically, the current study aims to examine the performance of MGCFA-ES as an effect-size in meta-analyses and evaluate it using a Monte Carlo simulation. In the simulation, the bias and mean square error (MSE) values, empirical Type I error rates, empirical statistical powers, coverage rates of 95% confidence intervals, and empirical standard errors are all evaluated as outcomes in relation to the following factors: (1) the type of correlation matrices, (2) the magnitudes of a DIF, (3) the level of an item difficulty, and (4) the sample size.

**Method**

For the simulation employed in the current study, it is assumed that six items are used to measure the underlying ability on a dichotomous scale, with 1 being a correct answer and 0 being an incorrect answer. Of the six items, it is assumed that one item displays DIF between the focal and reference groups with different magnitudes of difficulty ($b_F - b_R$).

**Data Generation**

Using the `sim` (‘irttoys’) function available in the R Version 3.5.3 (R Core Team, 2019), the response patterns on six items for a total $N_R + N_F$ observations (i.e., $N_R$ for reference and $N_F$ for focal groups, respectively) for 30 studies included in meta-analyses were generated based on test-takers’ ability level, which is assumed to be normally distributed with a mean of 0 and a standard deviation of 1 under the 1-PL (one-parameter logistic) model, where only $b$-parameters for the biased item are manipulated. For each of 30 included studies, we extracted three different types of correlation matrices from the response patterns of a total $N_R + N_F$ observations on six items, separately for the reference and focal groups. In addition, the threshold ($t_j$) for each item was obtained from the proportion of correct answers, which is used as a mean in the MGCFA.

For each individual study, the MGCFA model (as shown in Figure 1) was fitted to each type of correlation matrices using the `cfa` (‘lavaan’) function available in R Version 3.5.3 (R Core Team, 2019). The model was specified to be 1-PL by constraining all loadings, residuals, and thresholds to be constant for two groups, except the thresholds of a flagged item. The latent factor for the reference group was fixed to have a mean of 0 with a variance of 1, while the mean and variance of latent factor for the focal group were freely estimated (Millsap, 2012; Stark et al., 2006). The model parameters (i.e., loadings and thresholds) of MGCFA were converted to the item difficulty parameters using Equation 2, and the MGCFA-ES was computed via Equation 3 for each of the 30 included studies.

**Manipulating Factors in the Simulation**

**Item Parameters.** The values of $a$-parameters were fixed to 1.17 for all six items. The values of $b$-parameters for five unbiased items (Items 1-5) were normally distributed
with a mean of 0 and variance of 1, and three different conditions with low difficulty \((b = -1)\), medium difficulty \((b = 0)\), and high difficulty \((b = 1)\) were manipulated for the biased item (Item 6), which was modified within the range obtained from previous studies (e.g., Jin et al., 2012).

**DIF Magnitudes.** Followed by a simulation study by Jin et al. (2012), DIF magnitude for the biased item was manipulated with four different conditions: no DIF \((b_F - b_R = 0)\), small DIF \((b_F - b_R = .3)\), medium DIF \((b_F - b_R = .5)\), and large DIF \((b_F - b_R = .7)\).

**Sample Size.** Three different sample size levels were generated, including small \((N_F = 200, N_R = 400)\), medium \((N_F = 350, N_R = 700)\), and large \((N_F = 500, N_R = 1,000)\), which are reflective of real test settings by assigning the unbalanced sample sizes for the focal and reference groups (Jin et al., 2012).

**Correlation Type.** Three types of correlation matrices were extracted from item responses for focal and reference groups. In particular, the tetrachoric correlation has arisen as an alternative, since the Pearson product moment correlation is known to underestimate the true relationship between dichotomous items. Also, Fillmore et al. (1998) suggested transforming the Pearson correlation to a tetrachoric correlation by multiplying it by \(3/2\). Given that different correlation matrices can be used for MGCFA, the current study compared how the performance of MGCFA-ES for meta-analysis differs depending on the type of correlation (i.e., Pearson correlation, tetrachoric correlation, or adjusted Pearson correlation—Pearson correlation \(\times 3/2\) as suggested by Fillmore et al., 1998).

**Summary.** A total of 108 conditions were utilized in the current study, where MGCFA was fitted to three different correlation types generated from 36 item
response patterns with 500 replications, totaling 54,000 data points (i.e., \(108 \times 500\) replications).

**Meta-Analytic Estimator of MGCFA**

Figure 1 shows the MGCFA model for the current simulation study. Once MGCFA-ES and its associated standard errors are computed from each study, the population magnitude of DIF on the flagged item between focal and reference groups was estimated using the weighted average of MGCFA-ESs extracted from the individual studies, which can be computed as

\[
\text{MGCFA-ES} = \frac{\sum_{i=1}^{k} W_i [\text{MGCFA-ES}_i]}{\sum_{i=1}^{k} W_i},
\]

and

\[
V_{\text{MGCFA-ES}} = \frac{1}{\sum_{i=1}^{k} W_i},
\]

where \(k\) is the number of studies included in the meta-analysis and \(W_i\) is the inverse of the associated estimated variance of MGCFA-ES\(_i\). Below, MGCFA-ES\(_*\) is a meta-analytic estimator of all MGCFA effect sizes from individual studies (MGCFA-ES\(_i\)).

**Evaluation of Meta-Analytic Estimator of MGCFA-ES**

The performance of MGCFA-ES as the DIF index was evaluated using bias and \(MSE\) values, which are given by

\[
\text{Bias}(\hat{\theta}) = E(\hat{\theta}) - \theta,
\]

and

\[
\text{MSE}(\hat{\theta}) = [\text{Bias}(\hat{\theta})]^2 + \text{var}(\hat{\theta}),
\]

where \(\hat{\theta}\) is MGCFA-ES\(_*\) across all replications for each condition and \(\theta\) is the preset population value of DIF magnitude. Mean bias values of MGCFA-ES\(_*\), less than \(|\pm 0.05|\) were considered to be within an acceptable range (Hoogland & Boomsma, 1998). In addition, the coverage rate of 95% confidence intervals, empirical standard errors of the \(\hat{\theta}\) (\(\sqrt{\text{var}(\hat{\theta})}\)), and empirical rejection rates of MGCFA-ES\(_*\) were
computed. In order to control for the overall type I error rate, Bonferroni’s adjusted alpha level of .0083 was used (Kim & Oshima, 2012).

**Results**

**Performance of Meta-Analytic Estimator of MGCFA-ES**

The overall performances of MGCFA-ES are summarized below in terms of (1) empirical Type I error rates and statistical power, (2) bias and $MSE$ values, and (3) coverage rate of 95% confidence intervals and empirical standard errors.

**Type I Error Rates and Statistical Power.** Under the condition that DIF does not occur, the percentage rates of incorrectly rejecting the null hypothesis were 0.9%, which were all slightly above the preset nominal Type I error rate of .0083, regardless of correlation type. In addition, under the condition that DIF is set to occur, the mean percentages of correctly rejecting the null hypothesis were all equal to 100%. This result indicates that MGCFA-ES, as the DIF index, has sufficient statistical power for correctly detecting DIF on the biased item, regardless of the correlation type.

**Bias and $MSE$ values.** Figure 2 depicts bias and $MSE$ values of MGCFA-ES by correlation type. When a tetrachoric correlation was used, mean bias and $MSE$ values of MGCFA-ES were found to be the smallest (i.e., less than |.05|), indicating that MGCFA-ES extracted from a tetrachoric correlation yielded the most accurate estimate of the population magnitude of DIF. However, when a Pearson correlation was used, bias values of MGCFA-ES were higher than |.05|. Similarly, the $MSE$ value of MGCFA-ES was the smallest when MGCFA was fitted to tetrachoric correlations, followed by an adjusted Pearson correlation. Regardless of correlation type, mean bias, and $MSE$ values of MGCFA-ES were the largest when a large DIF appeared on the flagged item, followed by medium and small DIFs.

**Coverage of 95% Confidence Intervals and Empirical Standard Error.** Figure 2 shows coverage of 95% confidence intervals and empirical standard error for MGCFA-ES by correlation type and DIF magnitude. Regardless of DIF magnitude, coverage of 95% confidence intervals around MGCFA-ES was the largest when a tetrachoric correlation was used, while it was lowest for the Pearson correlation. The empirical standard errors of MGCFA-ES were all below .05 and were almost identical, though slightly less for the tetrachoric correlation.

**Factors Affecting Meta-Analytic Estimator of MGCFA-ES**

The differential effects of various factors on MGCFA-ES are summarized below in terms of (1) bias and $MSE$ values and (2) coverage rate of 95% confidence intervals and empirical standard errors.
Bias and MSE Values. As shown in Figure 3, the mean bias values of MGCFA-ES were found to be greatest for identifying an item showing a large difference in item response between focal and reference groups, followed by medium, small, and no DIF items. An exception was found when a tetrachoric correlation was used, showing the greatest mean bias values with no DIF item. As shown in Figure 4, the MSE values of MGCFA-ES were found to be greatest for identifying an item showing large DIF in responses between focal and reference groups, followed by medium, small, and no DIF items.

Coverages of 95% Confidence Intervals and Empirical Standard Error. As shown in Figure 5, coverage rates of MGCFA-ES were found to be greatest for identifying an item showing no difference in item responses, followed by small, medium, and large DIF items for the Pearson and adjusted Pearson correlations. For a tetrachoric correlation, the coverage rate was the largest for no DIF item, followed by large, medium, and small DIFs. Such a pattern was consistent across all levels of item difficulty. One exception was when coverage rate of MGCFA-ES was the largest for an item with small DIF when the sample size was set to be small. As shown in Figure 6, the empirical standard error of MGCFA-ES was found to be largest for identifying a large DIF item, followed by small, medium, and no DIF items. The pattern was consistent regardless of the types of correlation matrices.

Figure 2. The bias, MSE, confidence interval (CI) coverage rate, and empirical standard error (EmpSE) of the meta-analytic estimator of MGCFA-ES, when different correlation matrices were used to fit MGCFA.

Note. DIF = differential item functioning; Pearson = Pearson correlation matrices were used; Adjusted = Pearson correlation matrices × 3/2 were used; tetrachoric = Tetrachoric correlation matrices were used; MSE = mean square error; MGCFA-ES = multigroup confirmatory factor analysis effect sizes.
Figure 3. The bias of meta-analytic estimator of MGCFA-ES by difficulty and DIF, and sample size and DIF.

Note. DIF = differential item functioning condition; MGCFA-ES = multigroup confirmatory factor analysis effect sizes.
Figure 4. The MSE of meta-analytic estimator of MGCFA-ES by difficulty and DIF, and sample size and DIF.

Note. DIF = differential item functioning condition; MSE = mean square error; MGCFA-ES = multigroup confirmatory factor analysis effect sizes.
Figure 5. Confidence interval (CI) coverage rate of the meta-analytic estimator of MGCFA-ES by difficulty and DIF, and sample size and DIF.

Note. DIF = differential item functioning condition; MGCFA-ES = multigroup confirmatory factor analysis effect sizes.
Figure 6. Empirical standard error (EmpSE) of the meta-analytic estimator of MGCFA-ES by difficulty and DIF, and sample size and DIF. 

Note. DIF = differential item functioning condition; MGCFA-ES = multigroup confirmatory factor analysis effect sizes.
The current section describes how the proposed method can be utilized in practice. In this section, we assume five MGCFA-ESs between \( p \) subgroups (i.e., \( p = 2 \) in this demonstration) extracted from \( k \) independent studies (\( k = 5 \) in this demonstration) that provide (1) Pearson product moment correlation matrices and (2) the proportion of correct answers on each item. Below, the part of R codes (presented in italics) that are necessary for each step are presented.

**Step 1: Creating a Data Set.** As shown in Figure 7, three data sets are created: (1) the five sets of two correlation matrices among items stacked by rows (saved as “c.cor”), (2) the five sets of two proportions of correct answers on each item stacked by rows (saved as “c.mean”), and (3) the five sets of two separate sample sizes stacked by rows (saved as “c.n”). As shown in R code below, the five sets of two separate correlation matrices among items stacked by rows are corrected by multiplying by 3/2 in note 1. The five sets of two proportions of correct answers on each item are converted into a threshold value as shown in notes 2 and 3.

```r
for(i in 1:k){
c.cor.r=as.matrix(cor.r[(1 + 6*(i-1)):(6*i), 2:7])
c.cor.r1<-(-3/2)*(c.cor.r) # adjust Pearson correlation matrices (note #1).
diag(c.cor.r1)<-1

c.cor.f=as.matrix(cor.f[(1 + 6*(i-1)):(6*i), 2:7])
c.cor.f1<-(-3/2)*(c.cor.f)
diag(c.cor.f1)<-1
```

**Figure 7.** The data set for correlation matrices, the mean of correct answers on each item, and sample sizes.

**Application to Empirical Data Using R**

The current section describes how the proposed method can be utilized in practice. In this section, we assume five MGCFA-ESs between \( p \) subgroups (i.e., \( p = 2 \) in this demonstration) extracted from \( k \) independent studies (\( k = 5 \) in this demonstration) that provide (1) Pearson product moment correlation matrices and (2) the proportion of correct answers on each item. Below, the part of R codes (presented in italics) that are necessary for each step are presented.
Step 2: Fitting MGCFA to the Data Set. Using the cfa ("lavaan") available in the R Version 3.5.3 (R Core Team, 2019), the MGCFA model is specified to fit the data extracted from each study. In particular, thresholds for all items (x1 to x5) except a flagged item (x6) are fixed to be the same for the two groups, and factor scores (f1) are fixed to have means of zero and variances of 1 for the reference group while they were estimated freely for the focal group as shown in notes 4 to 7. Then, MGCFA-ES (DIF = b7–b6) and its associated standard error are estimated as shown in note 8. The specified model (model) is fitted using three data sets (c.cor, c.mean, and c.n) in the cfa ("lavaan") function as shown in note 9.

```
model <-`

  group: 1
  f1 =~ l1*x1 + l2*x2 + l3*x3 + l4*x4 + l5*x5 + l6*x6
  x1 ~~ residual*x1
  x2 ~~ residual*x2
  x3 ~~ residual*x3
  x4 ~~ residual*x4
  x5 ~~ residual*x5
  x6 ~~ residual*x6
  x1 ~ i1
  x2 ~ i2
  x3 ~ i3
  x4 ~ i4
  x5 ~ i5
  x6 ~ i6
  f1 ~~ 1*f1  # factor scores (f1) have a variance of 1 (note #4)
  f1~0*f1  # factor scores (f1) has a mean of 0 (note #5)

  group: 2
  f1 =~ l1*x1 + l2*x2 + l3*x3 + l4*x4 + l5*x5 + l6*x6
```
\[
x_1 \sim \text{residual}^* x_1 \\
x_2 \sim \text{residual}^* x_2 \\
x_3 \sim \text{residual}^* x_3 \\
x_4 \sim \text{residual}^* x_4 \\
x_5 \sim \text{residual}^* x_5 \\
x_6 \sim \text{residual}^* x_6 \\
x_1 \sim i_1^* l \\
x_2 \sim i_2^* l \\
x_3 \sim i_3^* l \\
x_4 \sim i_4^* l \\
x_5 \sim i_5^* l \\
x_6 \sim i_7^* l \\
f_1 \sim f_1 \ # \text{factor scores are estimated freely (note \#6)} \\
f_1 \sim f_1 \ # \text{factor scores are estimated freely (note \#7)} \\
a := 1.7^*(l)/\sqrt{\text{residual}} \\
b_1 := (i_1)/(l) \\
b_2 := (i_2)/(l) \ b_3 := (i_3)/(l) \\
b_4 := (i_4)/(l) \\
b_5 := (i_5)/(l) \\
b_6 := (i_6)/(l) \\
b_7 := (i_7)/(l) \\
DIF = b_7-b_6 \ # \text{define DIF (note \#8)} \\
\]

Require(lavaan) \# load library called lavaan.

\[
\text{fit.cor} = \text{cfa(model, sample.cov = c.cor, sample.mean=c.mean, sample.nobs = c.n, std.lv=TRUE)} \ # \text{run multiple group CFA using datasets (note \#9)}
\]

**Step 3: Meta-Analysis of MGCFA-ES.** The MGCFA-ESs and their associated standard errors for each study as estimated in Step 2 are combined using the \textit{rma}(“metafor”) available in the R Version 3.5.3 (R Core Team, 2019).

\[
\text{require(metafor) } \\
\text{RE.cor=rma(yi=DIF.cor$diff, sei=DIF.cor$se, data=DIF.cor, } \\
\text{measure="GEN", method="REML") } \\
\text{Summary(RE.cor)}
\]

**Conclusion and Discussion**

The current study (1) proposes a new meta-analytic index (MGCFA-ES) for synthesizing the magnitude of DIF across studies, when an MGCFA was used and (2) evaluates the performance of MGCFA-ES using a Monte Carlo Simulation technique, where a number of factors were manipulated. The meta-analytic summary of
MGCFA-ES was found to perform reasonably well in terms of the bias and MSE values, empirical Type I error rates, statistical power, coverage rates, and empirical standard error. Of the three types of correlations used to fit the MGCFA, tetrachoric correlation provided the most accurate and unbiased estimate, followed by the adjusted Pearson product moment correlation. In addition, the proposed meta-analytic approach for synthesizing DIF across studies was found to yield the most accurate estimator when a tetrachoric correlation was used to find the item, showing a large DIF. It was also found that the meta-analytic summary of MGCFA-ES was most efficient when a tetrachoric correlation based on a large sample size was used.

The current simulation study demonstrated that MGCFA-ES could be used to summarize the magnitude of DIF across studies included in meta-analyses, when studies provide correlation matrices and item thresholds summarizing responses for the known subgroups. The use of tetrachoric correlations yields the most accurate and efficient estimators of DIF when fitting MGCFA for measurement invariance. However, when Pearson correlation matrices were reported from the studies, adjusting them by multiplying by 3/2, as suggested by Fillmore et al. (1998), produced more accurate and unbiased results. As shown in the simulation results, the meta-analytic summary of MGCFA-ES extracted from the adjusted Pearson correlation performed almost the same as the meta-analytic summary of MGCFA-ES when tetrachoric correlations were fitted. Although the current study might be limited, as not all features of meta-analysis (i.e., the number of studies included was fixed to 30 and the fixed effect model was only investigated) were manipulated, we believe that our study clearly shows MGCFA-ES as a viable option for summarizing the magnitude of DIF in meta-analyses.

It is our belief that with more published studies using SEM for identifying items showing DIF in the future, MGCFA-ES shows great promise for wider use. We strongly recommend that researchers provide separate correlation matrices among items and the proportion of correct answers on each item. Further research is necessary to expand the current study so that the performance of MGCFA-ES can be evaluated under conditions that mirror different meta-analytic settings. For example, given that SEM studies are mostly based on larger sample sizes, we used a minimum sample size of 200 in our simulation. Yet the performance of the MGCFA-ES needs to be assessed when SEM studies with smaller sample sizes or more items are included. In addition, future studies should explore meta-analytic methods that can be used to detect a nonuniform DIF or DIF on polytomous items. Last, an empirical study that examines the comparability of different DIF effect size indicators is necessary to provide practical guidelines to meta-analysts.

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